

Calculating Powers



There is a short way of writing repeated multiplication by the same number :

	How you write it	How you say it
3×3	3^2	3 to the power 2 usually called 3 squared
$3 \times 3 \times 3$	3^3	3 to the power 3 usually called 3 cubed
$3 \times 3 \times 3 \times 3$	3^4	3 to the power 4 usually called 3 to the fourth

Exercise 1 Find the value of these powers :

$$5^2 = \dots\dots\dots$$

$$2^3 = \dots\dots\dots$$

$$10^5 = \dots\dots\dots$$

$$5^3 = \dots\dots\dots$$

$$3^4 = \dots\dots\dots$$

$$1^7 = \dots\dots\dots$$

$$10^6 = \dots\dots\dots$$

Multiplying powers of the same number

Sometimes you need to write the product of two or more powers of a number as a single power of the same number.

Example :

$$2^3 \times 2^2 = (2 \times 2 \times 2) \times (2 \times 2) = 2 \times 2 \times 2 \times 2 \times 2 = 2^5$$

Exercise 2 Write these expressions as a single power of the number :

$$2^2 \times 2^2 = \dots\dots\dots$$

$$3^4 \times 3^2 = \dots\dots\dots$$

$$7^2 \times 7^8 = \dots\dots\dots$$

$$13^2 \times 13 = \dots\dots\dots$$

$$2^2 \times 2^2 \times 2^3 = \dots\dots\dots$$

$$5^3 \times 5^2 \times 5 = \dots\dots\dots$$

Dividing powers of the same number

You can use a similar method when you divide one power of a number by another power of the same number

Example $\frac{5^6}{5^2} = \frac{5 \times 5 \times 5 \times 5 \times 5 \times 5}{5 \times 5} = 5 \times 5 \times 5 \times 5 = 5^4$

Exercise 3 Write these expressions as a single power of the number :

$$\frac{3^5}{3^3} = \dots\dots\dots$$

$$\frac{7^6}{7^3} = \dots\dots\dots$$

$$\frac{13^4}{13^3} = \dots\dots\dots$$

$$\frac{17^3}{17^3} = \dots\dots\dots$$

Raising a power of a number to a further power

Example

$$(2^4)^3 = (2 \times 2 \times 2 \times 2) \times (2 \times 2 \times 2 \times 2) \times (2 \times 2 \times 2 \times 2) = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 2^{12}$$

Exercise 4 Simplify these expressions by writing as a single power of the number

$$(3^2)^2 = \dots\dots\dots$$

$$(5^3)^2 = \dots\dots\dots$$

$$(5^2)^3 = \dots\dots\dots$$

$$(7^3)^4 = \dots\dots\dots$$

Exercise 5 Multiplying different numbers to the same power

Example

$$3^2 \times 5^2 = 3 \times 3 \times 5 \times 5 = 3 \times 5 \times 3 \times 5 = 15 \times 15 = 15^2$$

$$3^2 \times 2^2 = \dots\dots\dots$$

$$5^3 \times 2^3 = \dots\dots\dots$$

$$3^4 \times 10^4 = \dots\dots\dots$$

Powers of ten

Write as a power of ten and as a decimal number

$$10^5 \times 10^4 = \dots\dots\dots$$

$$10^3 \times 10^2 \times 10 = \dots\dots\dots$$

$$\frac{10^6}{10^4} = \dots\dots\dots$$

$$\frac{10^7}{10^6} = \dots\dots\dots$$

$$\frac{10^5}{10^5} = \dots\dots\dots$$

$$\frac{10^5}{10^6} = \dots\dots\dots$$

$$\frac{10^3}{10^5} = \dots\dots\dots$$

$$\frac{10^3}{10^{10}} = \dots\dots\dots$$

$$10^6 \times 10^6 = \dots\dots\dots$$

$$\frac{10^5 \times 10^4}{10^3} = \dots\dots\dots$$

$$\frac{10^3 \times 10^4}{10^5 \times 10^2} = \dots\dots\dots$$

$$\frac{10^2 \times 10^3}{10^4 \times 10^2} = \dots\dots\dots$$

$$\frac{(10^3)^2}{10^2 \times 10^2} = \dots\dots\dots$$

$$\frac{(10^2)^2}{(10^3)^3} = \dots\dots\dots$$

Write as decimal number

$10^5 = \dots\dots\dots$	$10^3 = \dots\dots\dots$	$10^9 = \dots\dots\dots$	$10^1 = \dots\dots\dots$
$10^0 = \dots\dots\dots$	$10^{-1} = \dots\dots\dots$	$10^{-2} = \dots\dots\dots$	$10^{-5} = \dots\dots\dots$